

## Mathematics Common Core Sample Questions

Domain: Operations and Algebraic Thinking
Item: CR

1 Candy wants to buy herself a new bicycle that costs $\$ 240$. Candy has already saved She decides to save the same amount of money, $x$ dollars, each month for the next four months.

Part A: Write an equation that helps Candy determine the amount of money she must save each month.

## Equation

$\qquad$

Part B: Solve the equation to find the amount of money she must save each month to meet her goal of buying a bicycle.

Show your work.

Answer \$ $\qquad$

Key:
Part A: $\frac{(240-32)}{4}=x$ or $32+4 x=240$ or equivalent equation

Part B: $\quad \frac{(240-32)}{4}=x$

$$
\frac{208}{4}=x
$$

$$
52=x
$$

or other valid process.

## AND

Answer: \$52
Aligned CCLS: 4.OA. 3
Commentary: This question aligns to CCLS 4.OA. 3 and assesses a student's ability to solve a multi-step word problem posed with whole numbers. It also assesses the ability to represent a problem using an equation with a letter standing for the unknown quantity.

Rationale: In Part A the equation includes the subtraction of $\$ 32$ from $\$ 240$ to identify how much is needed to be saved in four months and the division of the remaining amount, $\$ 208$, by four to represent the amount to be saved each month. Likely errors may include dividing $\$ 240$ by four without subtracting the already saved amount of $\$ 32$ $\left(\frac{240}{4}=60\right)$ or using $\$ 32$ dollars as the amount of money saved during the first month and dividing the remaining amount by three $\left(\frac{(240-32)}{3}=69 . \overline{33}\right)$. In Part B errors may occur during the computation of the equation in Part A or may be the result of accurate computations based on an inaccurate equation from Part $A$.

Domain: Operations and Algebraic Thinking
Item: CR
2 Students from three classes at Hudson Valley Elementary School are planning a boat trip. On the trip, there will be 20 students from each class, along with 11 teachers and 13 parents.

Part A: Write an equation that can be used to determine the number of boats, $b$, they will need on their trip if 10 people ride in each boat.

Equation: $b=$ $\qquad$

Part B: How many boats will be needed for the trip if 10 people ride in each boat?

## Show your work.

Answer: $\qquad$ boats

Part C: It will cost $\$ 35$ to rent each boat used for the trip. How much will it cost to rent all the boats needed for the trip?

Show your work.

Answer: \$ $\qquad$

## Key:

Part A: $\quad b=\frac{[20(3)+11+13]}{10}$
Part B: Work:
$b=\frac{84}{10}$
$b=8 \mathrm{R} 4$

The number of boats needed is $8+1=9$ boats

Answer: 9 boats

Part C: Total Cost $=35 \times 9=315$

Answer: \$315

## Aligned CCLS: 4.OA. 3

Commentary: This question aligns to CCLS 4.OA. 3 and assesses a student's ability to solve a multi-step word problem posed with whole numbers. It also tests the student's ability to represent the problem using an equation, with a letter standing for the unknown quantity. It tests a student's ability to interpret the remainder of the division problem and use this interpretation properly to determine the number of boats as well as the total cost.

Rationale: The equation in Part A includes a calculation for the number of students who went on the trip $(20 \times 3=60)$ plus the 11 teachers and 13 parents, bringing the total to 84 individuals on the trip. The number of boats, $b$, needed is the sum of all individuals divided by the number of people able to sit in a single boat. In Part B, students perform the calculation -84 is divided by 10 , to get 8 R 4 . The remainder of 4 indicates that an additional boat is needed, so the number of boats needed is $8+1=9$ boats. In Part C , the total cost is the number of boats required multiplied by the cost per boat, $\$ 35 \times 9=\$ 315$.

Domain: Number and Operations-Fractions
Item: CR

3 Elena, Matthew, and Kevin painted a wall. Elena painted $\frac{5}{9}$ of the wall and Matthew painted $\frac{3}{9}$ of the wall. Kevin painted the rest of the wall.

Part A: Use the box below to represent the wall. Show the fraction of the wall that Kevin painted.


Part B: What fraction of the wall did Kevin paint? $\qquad$

Key:

## Part A:



AND
Part B: $\frac{1}{9}$

## Aligned CCLS: 4.NF.3d

Commentary: This question is aligned with CCLS 4.NF.3d and assesses a student's ability to solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators by using visual fraction models and equations to represent the problem.

Rationale: The wall should be partitioned into nine equal pieces, and the portion Kevin painted should be indicated. Determining the fraction Kevin painted may be solely completed via the visual model. However, the use of equations may also be used to determine the fraction Kevin painted. Matthew and Elena completed $\frac{5}{9}+\frac{3}{9}=\frac{8}{9}$. Since the entire job represents 1 whole, $\frac{8}{9}$ is subtracted from $1\left(1-\frac{8}{9}=\frac{1}{9}\right)$.

Domain: Measurement and Data
Item: CR

4 The area of Ken's rectangular garden is 480 square feet. The garden is 24 feet wide. completely on all four sides?

Show your work.

Answer: $\qquad$ feet

Key:
Length of the garden: $\frac{480}{24}=20$ feet

Perimeter: $2 \times(20+24)=88$ feet
Answer: 88 feet.

Aligned CCLS: 4.MD. 3

Commentary: This question aligns to CCLS 4.MD. 3 because it assesses a student's ability to apply the area and perimeter formulas in a real-world situation.

Rationale: Using the formula area = length $\times$ width, the length of the garden can be found by solving the equation ( $480=$ length $\times 24$ ), dividing the area by the width of the garden: $\frac{480}{24}=20$. Calculating the length of fencing needed to surround the garden on all four sides requires the use of both length and width: $2 \times(20+24)=88$ feet.

Domain: Measurement and Data
Item: CR
5 Lisa recorded the approximate amount of time, in hours, it took her to do her homework each day for 15 days.

$$
\frac{1}{4}, \frac{1}{2}, 0,1, \frac{3}{4}, \frac{1}{4}, \frac{1}{2}, 0,1, \frac{3}{4}, \frac{1}{4}, \frac{1}{4}, \frac{3}{4}, 0, \frac{1}{4}
$$

In the space below, create a line plot to represent Lisa's data. Be sure to label the $x$-axis and title the line plot.

## Key:

Lisa's Approximate Homework Times (in hours)

|  | $x$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $x$ |  |  |  |
| $x$ | $x$ |  | $x$ |  |
| $x$ | $x$ | $x$ | $x$ | $x$ |
| $x$ | $x$ | $x$ | $x$ | $x$ |
| 0 | $\frac{1}{4}$ | $\frac{1}{2}$ | $\frac{3}{4}$ | 1 |

## Aligned CCLS: 4.MD. 4

Commentary: This question aligns to CCLS 4.MD.4. It assesses a student's ability to display a data set of measurements in fractions of a unit and make a line plot to display that data.

Rationale: The set of data contains five unique values, including the fractions $\frac{1}{4}, \frac{1}{2}$, and $\frac{3}{4}$. All of these values are plotted on the number line, and each occurrence of that number receives an $x$ to represent each unique occurrence. The axis should be properly labeled, and the line plot titled.

Domain: Operations and Algebraic Thinking
Item: MC

6 Which of the number patterns below follows the rule subtract 7 to get to the next number?

A 79, 72, 56, 51, 47, 44
B $66,60,53,45,36,26$
C $51,44,37,30,23,16$
D $43,36,29,24,19,12$

Key: C

Aligned CCLS: 4.OA. 5
Commentary: This question is aligned to CCLS 4.OA. 5 and assesses a student's ability to generate a number pattern, based upon a given rule.

Rationale: The correct answer is Option C, because each successive term is created by the rule "subtract 7." The pattern in Option C is "subtract 7," or $51-44=7$, 44-37 = 7, and so on. An answer of Option A or D would most likely indicate that the student did not test to see if the pattern explained how every term in the sequence was generated. Selecting Option B would most likely indicate a mistake in subtraction or application of the rule.

Domain: Operations and Algebraic Thinking
Item: MC
7 The first five terms in a shape pattern are shown below. The rule of the pattern is the number of circles increases by three. Which of the following would be true of the 6th term?
$\infty 0$


A The number of circles in the 6th term would be a multiple of four.
B The number of circles in the 6th term would be a prime number.
C The number of circles in the 6th term would be an even number.
D The number of circles in the 6th term would be divisible by five.

## Key: C

Aligned CCLS: 4.OA. 5

Commentary: This question is aligned with CCLS 4.OA. 5 and assesses a student's ability to identify apparent features of the pattern that were not explicit in the rule itself.

Rationale: The correct answer is Option C, because the addition of three more circles to the fifteen in the 5th term will result in an even number, 18. Option A could indicate a misunderstanding of the concept of multiple. Option B could indicate a misunderstanding of the concept of prime number, or may indicate an inaccurate association between the value of three in the rule with three being a prime number. Option D may indicate an application of the claim in Option D on the fifth term rather than on the unrepresented sixth term.

Domain: Operations and Algebraic Thinking/Number and Operations-Fractions Item: MC

8
A high school basketball team scored a total of 108 points in their final game. Joanne scored exactly $\frac{1}{3}$ of all the points the team scored, and Renee scored 23 points. How many points were scored by the rest of the team?

A 36
B 49
C 59
D 85

## Key: B

Aligned CCLS: 4.OA.3, 4.NF.4c

Commentary: This question is aligned with CCLS 4.NF.4c and 4.OA.3. It assesses a student's ability to multiply a fraction by a whole number and to solve a multi-step word problem using addition and subtraction of whole numbers.

Rationale: The correct choice, Option B, is found by computing $\frac{1}{3} \times 108=36$, which is the number of points scored by Joanne. Since Renee scored 23 points, the total points scored by the two girls is $36+23=59$ points. Then $108-59=49$, the number of points scored by the rest of the team. If students miss the last step, they may select Option C. If they miss the last two steps, they may select Option A. If they simply subtract $108-23$, they will get Option D.

Domain: Operations and Algebraic Thinking
Item: MC
9 Jim baked sugar cookies and peanut butter cookies. He baked 8 sugar cookies and 3 times as many peanut butter cookies. What is the total number of cookies that Jim baked?

A 11
B 24
C 32
D 40

Key: C

Aligned CCLS: 4.OA. 2
Commentary: This question is aligned to CCLS 4.OA. 2 because it assesses a student's ability to multiply in order to solve a word problem that also includes a multiplicative comparison (3 times as many).

Rationale: Option C is the correct answer. Jim baked $3 \times 8=24$ peanut butter cookies, and since he also baked 8 sugar cookies, the total number of cookies baked is $24+8=32$. Selecting Option B as the correct answer indicates that the 8 sugar cookies were not added to the number of peanut butter cookies to get the total number of cookies. Option A indicates a simple addition $(8+3=11)$ that does not incorporate the claim that there are 3 times as many peanut butter cookies as sugar cookies. Option D may indicate miscalculations throughout the process.

# Grade 4 <br> Mathematics <br> Common Core Sample Questions 

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